

# Evolutionary Computation: Comments on the History and Current State

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**Abstract**— Evolutionary computation has started to receive significant attention during the last decade, although the origins can be traced back to the late 1950's. This article surveys the history as well as the current state of this rapidly growing field. We describe the purpose, the general structure, and the working principles of different approaches, including genetic algorithms (GA) [with links to *genetic programming* (GP) and *classifier systems* (CS)], *evolution strategies* (ES), and *evolutionary programming* (EP) by analysis and comparison of their most important constituents (i.e., representations, variation operators, reproduction, and selection mechanism). Finally, we give a brief overview on the manifold of application domains, although this necessarily must remain incomplete.

**Index Terms**— Classifier systems, evolution strategies, evolutionary computation, evolutionary programming, genetic algorithms, genetic programming.

## I. EVOLUTIONARY COMPUTATION: ROOTS AND PURPOSE

THIS first issue of the IEEE TRANSACTIONS ON EVOLUTIONARY COMPUTATION marks an important point in the history of the rapidly growing field of evolutionary computation, and we are glad to participate in this event. In preparation for this summary, we strove to provide a comprehensive review of both the history and the state of the art in the field for both the novice and the expert in evolutionary computation. Our selections of material are necessarily subjective, and we regret any significant omissions.

Although the origins of evolutionary computation can be traced back to the late 1950's (see e.g., the influencing works of Bremermann [1], Friedberg [2], [3], Box [4], and others), the field remained relatively unknown to the broader scientific community for almost three decades. This was largely due to the lack of available powerful computer platforms at that time, but also due to some methodological shortcomings of those early approaches (see, e.g., Fogel [5, p. 103]).

The fundamental work of Holland [6], Rechenberg [7], Schwefel [8], and Fogel [9] served to slowly change this picture during the 1970's, and we currently observe a remarkable

and steady (still exponential) increase in the number of publications (see, e.g., the bibliography of [10]) and conferences in this field, a clear demonstration of the scientific as well as economic relevance of this subject matter.

But what are the benefits of evolutionary computation (compared to other approaches) which may justify the effort invested in this area? We argue that the most significant advantage of using evolutionary search lies in the gain of flexibility and adaptability to the task at hand, in combination with robust performance (although this depends on the problem class) and global search characteristics. In fact, evolutionary computation should be understood as a general adaptable concept for problem solving, especially well suited for solving difficult optimization problems, rather than a collection of related and ready-to-use algorithms.

The majority of current implementations of evolutionary algorithms descend from three strongly related but independently developed approaches: *genetic algorithms*, *evolutionary programming*, and *evolution strategies*.

Genetic algorithms, introduced by Holland [6], [11], [12], and subsequently studied by De Jong [13]–[16], Goldberg [17]–[21], and others such as Davis [22], Eshelman [23], [24], Forrest [25], Grefenstette [26]–[29], Koza [30], [31], Mitchell [32], Riolo [33], [34], and Schaffer [35]–[37], to name only a few, have been originally proposed as a general model of adaptive processes, but by far the largest application of the techniques is in the domain of optimization [15], [16]. Since this is true for all three of the mainstream algorithms presented in this paper, we will discuss their capabilities and performance mainly as optimization strategies.

Evolutionary programming, introduced by Fogel [9], [38] and extended in Burgin [39], [40], Atmar [41], Fogel [42]–[44], and others, was originally offered as an attempt to create artificial intelligence. The approach was to evolve finite state machines (FSM) to predict events on the basis of former observations. An FSM is an abstract machine which transforms a sequence of input symbols into a sequence of output symbols. The transformation depends on a finite set of states and a finite set of state transition rules. The performance of an FSM with respect to its environment might then be measured on the basis of the machine's prediction capability, i.e., by comparing each output symbol with the next input symbol and measuring the worth of a prediction by some payoff function.

Evolution strategies, as developed by Rechenberg [45], [46] and Schwefel [47], [48], and extended by Herdy [49], Kursawe [50], Ostermeier [51], [52], Rudolph [53], Schwefel [54], and

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others, were initially designed with the goal of solving difficult discrete and continuous, mainly experimental [55], parameter optimization problems.

During the 1980's, advances in computer performance enabled the application of evolutionary algorithms to solve difficult real-world optimization problems, and the solutions received a broader audience. In addition, beginning in 1985, international conferences on the techniques were offered (mainly focusing on genetic algorithms [56]–[61], with an early emphasis on evolutionary programming [62]–[66], as small workshops on theoretical aspects of genetic algorithms [67]–[69], as a genetic programming conference [70], with the general theme of problem solving methods gleaned from nature [71]–[74], and with the general topic of evolutionary computation [75]–[78]). But somewhat surprisingly, the researchers in the various disciplines of evolutionary computation remained isolated from each other until the meetings in the early 1990's [59], [63], [71].

The remainder of this paper is intended as an overview of the current state of the field. We cannot claim that this overview is close to complete. As good starting points for further studies we recommend [5], [18], [22], [31], [32], [48], and [79]–[82]. In addition moderated mailing lists<sup>1</sup> and newsgroups<sup>2</sup> allow one to keep track of current events and discussions in the field.

In the next section we describe the application domain of evolutionary algorithms and contrast them with the traditional approach of mathematical programming.

## II. OPTIMIZATION, EVOLUTIONARY COMPUTATION, AND MATHEMATICAL PROGRAMMING

In general, an optimization problem requires finding a setting  $\vec{x} \in M$  of free parameters of the system under consideration, such that a certain quality criterion  $f: M \rightarrow \mathbb{R}$  (typically called the *objective function*) is maximized (or, equivalently, minimized)

$$f(\vec{x}) \rightarrow \max. \quad (1)$$

The objective function might be given by real-world systems of arbitrary complexity. The solution to the *global* optimization problem (1) requires finding a vector  $\vec{x}^*$  such that  $\forall \vec{x} \in M: f(\vec{x}) \leq f(\vec{x}^*) = f^*$ . Characteristics such as *multimodality*, i.e., the existence of several *local maxima*  $\vec{x}'$  with

$$\exists \varepsilon > 0: \forall \vec{x} \in M: \rho(\vec{x}, \vec{x}') < \varepsilon \Rightarrow f(\vec{x}) \leq f(\vec{x}') \quad (2)$$

(where  $\rho$  denotes a distance measure on  $M$ ), *constraints*, i.e., restrictions on the set  $M$  by functions  $g_j: M \rightarrow \mathbb{R}$  such that the set of *feasible* solutions  $F \subseteq M$  is only a subset of the domain of the variables

$$F = \{\vec{x} \in M \mid g_j(\vec{x}) \geq 0 \forall j\} \quad (3)$$

and other factors, such as large dimensionality, strong nonlinearities, nondifferentiability, and noisy and time-varying

<sup>1</sup>For example, GA-List-Request@AIC.NRL.NAVY.MIL and EP-List-Request@magenta.me.fau.edu.

<sup>2</sup>For example, comp.ai.genetic.

objective functions, frequently lead to difficult if not unsolvable optimization tasks (see [83, p. 6]). But even in the latter case, the identification of an improvement of the currently known best solution through optimization is often already a big success for practical problems, and in many cases evolutionary algorithms provide an efficient and effective method to achieve this.

Optimization problems occur in many technical, economic, and scientific projects, like cost-, time-, and risk-minimization or quality-, profit-, and efficiency-maximization [10], [22] (see also [80, part G]). Thus, the development of general strategies is of great value.

In real-world situations the objective function  $f$  and the constraints  $g_j$  are often not analytically treatable or are even not given in closed form, e.g., if the function definition is based on a simulation model [84], [85].

The traditional approach in such cases is to develop a formal model that resembles the original functions close enough but is solvable by means of traditional mathematical methods such as linear and nonlinear programming. This approach most often requires simplifications of the original problem formulation. Thus, an important aspect of mathematical programming lies in the design of the formal model.

No doubt, this approach has proven to be very successful in many applications, but has several drawbacks which motivated the search for novel approaches, where evolutionary computation is one of the most promising directions. The most severe problem is that, due to oversimplifications, the computed solutions do not solve the original problem. Such problems, e.g., in the case of simulation models, are then often considered unsolvable.

The fundamental difference in the evolutionary computation approach is to adapt the method to the problem at hand. In our opinion, evolutionary algorithms should not be considered as off-the-peg, ready-to-use algorithms but rather as a general concept which can be tailored to most of the real-world applications that often are beyond solution by means of traditional methods. Once a successful EC-framework has been developed it can be incrementally adapted to the problem under consideration [86], to changes of the requirements of the project, to modifications of the model, and to the change of hardware resources.

## III. THE STRUCTURE OF AN EVOLUTIONARY ALGORITHM

Evolutionary algorithms mimic the process of natural evolution, the driving process for the emergence of complex and well-adapted organic structures. To put it succinctly and with strong simplifications, evolution is the result of the interplay between the creation of new genetic information and its evaluation and selection. A single individual of a population is affected by other individuals of the population (e.g., by food competition, predators, and mating), as well as by the environment (e.g., by food supply and climate). The better an individual performs under these conditions the greater is the chance for the individual to live for a longer while and generate offspring, which in turn inherit the (disturbed) parental genetic information. Over the course of evolution, this leads to a

penetration of the population with the genetic information of individuals of above-average fitness. The nondeterministic nature of reproduction leads to a permanent production of novel genetic information and therefore to the creation of differing offspring (see [5], [79], and [87] for more details).

This neo-Darwinian model of organic evolution is reflected by the structure of the following general evolutionary algorithm.

*Algorithm 1:*

```

t := 0;
initialize P(t);
evaluate P(t);
while not terminate do
  P'(t) := variation [P(t)];
  evaluate [P'(t)];
  P(t+1) := select [P'(t) ∪ Q];
  t := t + 1;
od

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In this algorithm,  $P(t)$  denotes a population of  $\mu$  individuals at generation  $t$ .  $Q$  is a special set of individuals that might be considered for selection, e.g.,  $Q = P(t)$  (but  $Q = \emptyset$  is possible as well). An offspring population  $P'(t)$  of size  $\lambda$  is generated by means of variation operators such as recombination and/or mutation (but others such as inversion [11, pp. 106–109] are also possible) from the population  $P(t)$ . The offspring individuals are then evaluated by calculating the objective function values  $f(\vec{x}_k)$  for each of the solutions  $\vec{x}_k$  represented by individuals in  $P'(t)$ , and selection based on the fitness values is performed to drive the process toward better solutions. It should be noted that  $\lambda = 1$  is possible, thus including so-called *steady-state* selection schemes [88], [89] if used in combination with  $Q = P(t)$ . Furthermore, by choosing  $1 \leq \lambda \leq \mu$  an arbitrary value of the *generation gap* [90] is adjustable, such that the transition between strictly generational and steady-state variants of the algorithm is also taken into account by the formulation offered here. It should also be noted that  $\lambda > \mu$ , i.e., a reproduction surplus, is the normal case in nature.

#### IV. DESIGNING AN EVOLUTIONARY ALGORITHM

As mentioned, at least three variants of evolutionary algorithms have to be distinguished: genetic algorithms, evolutionary programming, and evolution strategies. From these (“canonical”) approaches innumerable variants have been derived. Their main differences lie in:

- the representation of individuals;
- the design of the variation operators (mutation and/or recombination);
- the selection/reproduction mechanism.

In most real-world applications the search space is defined by a set of objects, e.g., processing units, pumps, heaters, and coolers of a chemical plant, each of which have different parameters such as energy consumption, capacity, etc. Those parameters which are subject to optimization constitute the so-called *phenotype space*. On the other hand the genetic

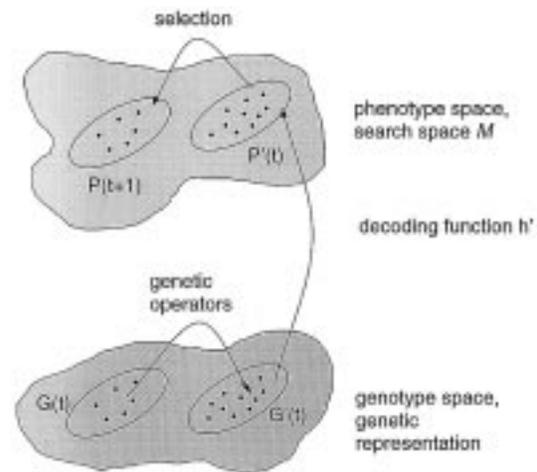


Fig. 1. The relation of genotype space and phenotype space [5, p. 39].

operators often work on abstract mathematical objects like binary strings, the *genotype space*. Obviously, a mapping or coding function between the phenotype and genotype space is required. Fig. 1 sketches the situation (see also [5, pp. 38–43]).

In general, two different approaches can be followed. The first is to choose one of the standard algorithms and to design a decoding function according to the requirements of the algorithm. The second suggests designing the representation as close as possible to the characteristics of the phenotype space, almost avoiding the need for a decoding function.

Many empirical and theoretical results are available for the standard instances of evolutionary algorithms, which is clearly an important advantage of the first approach, especially with regard to the reuse and parameter setting of operators. On the other hand, a complex coding function may introduce additional nonlinearities and other mathematical difficulties which can hinder the search process substantially [79, pp. 221–227], [82, p. 97].

There is no general answer to the question of which one of the two approaches mentioned above to follow for a specific project, but many practical applications have shown that the best solutions could be found after imposing substantial modifications to the standard algorithms [86]. We think that most practitioners prefer natural, problem-related representations. Michalewicz [82, p. 4] offers:

It seems that a “natural” representation of a potential solution for a given problem plus a family of applicable “genetic” operators might be quite useful in the approximation of solutions of many problems, and this nature-modeled approach . . . is a promising direction for problem solving in general.

Furthermore, many researchers also use hybrid algorithms, i.e., combinations of evolutionary search heuristics and traditional as well as knowledge-based search techniques [22, p. 56], [91], [92].

It should be emphasized that all this becomes possible because the requirements for the application of evolutionary heuristics are so modest compared to most other search techniques. In our opinion, this is one of the most important strengths of the evolutionary approach and one of the rea-

sons for the popularity evolutionary computation has gained throughout the last decade.

### A. The Representation

Surprisingly, despite the fact that the representation problem, i.e., the choice or design of a well-suited genetic representation for the problem under consideration, has been described by many researchers [82], [93], [94] only few a publications explicitly deal with this subject except for specialized research directions such as *genetic programming* [31], [95], [96] and the evolution of neural networks [97], [98].

Canonical genetic algorithms use a binary representation of individuals as fixed-length strings over the alphabet  $\{0, 1\}$  [11], such that they are well suited to handle pseudo-Boolean optimization problems of the form

$$f: \{0, 1\}^\ell \rightarrow \mathbb{R}. \quad (4)$$

Sticking to the binary representation, genetic algorithms often enforce the utilization of encoding and decoding functions  $h: M \rightarrow \{0, 1\}^\ell$  and  $h': \{0, 1\}^\ell \rightarrow M$  that facilitate mapping solutions  $\vec{x} \in M$  to binary strings  $h(\vec{x}) \in \{0, 1\}^\ell$  and vice versa, which sometimes requires rather complex mappings  $h$  and  $h'$ . In case of continuous parameter optimization problems, for instance, genetic algorithms typically represent a real-valued vector  $\vec{x} \in \mathbb{R}^n$  by a binary string  $\vec{y} \in \{0, 1\}^\ell$  as follows: the binary string is logically divided into  $n$  segments of equal length  $\ell'$  (i.e.,  $\ell = n \cdot \ell'$ ), each segment is decoded to yield the corresponding integer value, and the integer value is in turn linearly mapped to the interval  $[u_i, v_i] \subset \mathbb{R}$  (corresponding with the  $i$ th segment of the binary string) of real values [18].

The strong preference for using binary representations of solutions in genetic algorithms is derived from *schema theory* [11], which analyzes genetic algorithms in terms of their expected schema sampling behavior under the assumption that mutation and recombination are detrimental. The term *schema* denotes a similarity template that represents a subset of  $\{0, 1\}^\ell$ , and the *schema theorem* of genetic algorithms offers that the canonical genetic algorithm provides a near-optimal sampling strategy (in terms of minimizing expected losses) for schemata by increasing the number of well-performing, short (i.e., with small distance between the left-most and right-most defined position), and low-order (i.e., with few specified bits) schemata (so-called building blocks) over subsequent generations (see [18] for a more detailed introduction to the schema theorem). The fundamental argument to justify the strong emphasis on binary alphabets is derived from the fact that the number of schemata is maximized for a given finite number of search points under a binary alphabet [18, pp. 40–41]. Consequently, the schema theory presently seems to favor binary representations of solutions (but see [99] for an alternative view and [100] for a transfer of schema theory to  $S$ -expression representations used in genetic programming).

Practical experience, as well as some theoretical hints regarding the binary encoding of continuous object variables [101]–[105], however, indicate that the binary representation has some disadvantages. The coding function might introduce

an additional multimodality, thus making the combined objective function  $f = f' \circ h'$  (where  $f': M \rightarrow \mathbb{R}$ ) more complex than the original problem  $f'$  was. In fact, the schema theory relies on approximations [11, pp. 78–83] and the optimization criterion to minimize the *overall* expected loss (corresponding to the sum of all fitness values of all individuals ever sampled during the evolution) rather than the criterion to maximize the best fitness value ever found [15]. In concluding this brief excursion into the theory of canonical genetic algorithms, we would like to emphasize the recent work by Vose [106]–[109] and others [110], [111] on modeling genetic algorithms by Markov chain theory. This approach has already provided a remarkable insight into their convergence properties and dynamical behavior and led to the development of so-called *executable models* that facilitate the direct simulation of genetic algorithms by Markov chains for problems of sufficiently small dimension [112], [113].

In contrast to genetic algorithms, the representation in *evolution strategies* and *evolutionary programming* is directly based on real-valued vectors when dealing with continuous parameter optimization problems of the general form

$$f: M \subseteq \mathbb{R}^n \rightarrow \mathbb{R}. \quad (5)$$

Both methods have originally been developed and are also used, however, for combinatorial optimization problems [42], [43], [55]. Moreover, since many real-world problems have complex search spaces which cannot be mapped “canonically” to one of the representations mentioned so far, many strategy variants, e.g., for integer [114], mixed-integer [115], structure optimization [116], [117], and others [82, ch. 10], have been introduced in the literature, but exhaustive comparative studies especially for nonstandard representations are still missing. The actual development of the field is characterized by a progressing integration of the different approaches, such that the utilization of the common labels “genetic algorithm,” “evolution strategy,” and “evolutionary programming” might be sometimes even misleading.

### B. Mutation

Of course, the design of variation operators has to obey the mathematical properties of the chosen representation, but there are still many degrees of freedom.

Mutation in genetic algorithms was introduced as a dedicated “background operator” of small importance (see [11, pp. 109–111]). Mutation works by inverting bits with very small probability such as  $p_m = 0.001$  [13],  $p_m \in [0.005, 0.01]$  [118], or  $p_m = 1/\ell$  [119], [120]. Recent studies have impressively clarified, however, that much larger mutation rates, decreasing over the course of evolution, are often helpful with respect to the convergence reliability and velocity of a genetic algorithm [101], [121], and that even self-adaptive mutation rates are effective for pseudo-Boolean problems [122]–[124].

Originally, mutation in evolutionary programming was implemented as a random change (or multiple changes) of the description of the finite state machines according to five different modifications: change of an output symbol, change of a state transition, addition of a state, deletion of a state, or change

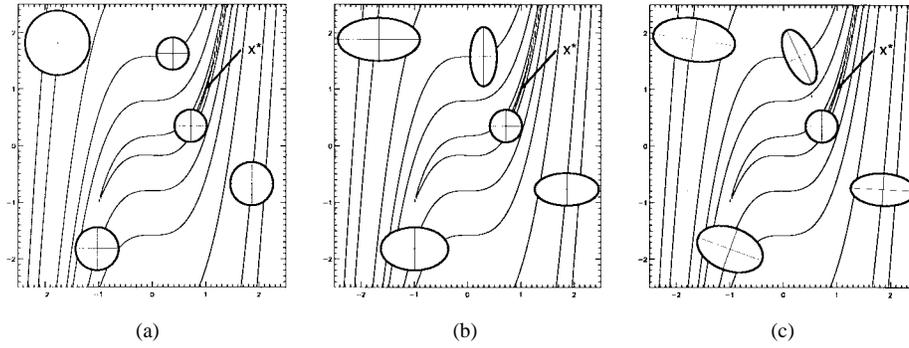


Fig. 2. Two-dimensional contour plot of the effect of the mutation operator in case of self-adaptation of (a) a single step size, (b)  $n$  step sizes, and (c) covariances.  $x^*$  denotes the optimizer. The ellipses represent one line of equal probability to place an offspring that is generated by mutation from the parent individual located at the center of the ellipses. Five sample individuals are shown in each of the plots.

of the initial state. The mutations were typically performed with uniform probability, and the number of mutations for a single offspring was either fixed or also chosen according to a probability distribution. Currently, the most frequently used mutation scheme as applied to real-valued representations is very similar to that of evolution strategies.

In evolution strategies, the individuals consist of object variables  $x_i \in \mathbb{R}$  ( $1 \leq i \leq n$ ) and so-called *strategy parameters*, which are discussed in the next section. Mutation is then performed independently on each vector element by adding a normally distributed random value with expectation zero and standard deviation  $\sigma$  (the notation  $N_i(\cdot, \cdot)$  indicates that the random variable is sampled anew for each value of the index  $i$ )

$$x'_i = x_i + \sigma \cdot N_i(0, 1). \quad (6)$$

This raises the question of how to control the so-called step size  $\sigma$  of (6), which is discussed in the next section.

### C. Self-Adaptation

In [125] Schwefel introduced an endogenous mechanism for step-size control by incorporating these parameters into the representation in order to facilitate the evolutionary *self-adaptation* of these parameters by applying evolutionary operators to the object variables and the strategy parameters for mutation at the same time, i.e., searching the space of solutions and strategy parameters simultaneously. This way, a suitable adjustment and diversity of mutation parameters should be provided under arbitrary circumstances.

More formally, an individual  $\vec{a} = (\vec{x}, \vec{\sigma})$  consists of object variables  $\vec{x} \in \mathbb{R}^n$  and strategy parameters  $\vec{\sigma} \in \mathbb{R}_+^n$ . The mutation operator works by adding a normally distributed random vector  $\vec{z} \in \mathbb{R}^n$  with  $z_i \sim N(0, \sigma_i^2)$  (i.e., the components of  $\vec{z}$  are normally distributed with expectation zero and variance  $\sigma_i^2$ ).

The effect of mutation is now defined as

$$\sigma'_i = \sigma_i \cdot \exp[\tau' \cdot N(0, 1) + \tau \cdot N_i(0, 1)] \quad (7)$$

$$x'_i = x_i + \sigma'_i \cdot N_i(0, 1) \quad (8)$$

where  $\tau' \propto (\sqrt{2n})^{-1}$  and  $\tau \propto (\sqrt{2\sqrt{n}})^{-1}$ .

This mutation scheme, which is most frequently used in evolution strategies, is schematically depicted (for  $n = 2$ )

in the middle of Fig. 2. The locations of equal probability density for descendants are concentric hyperellipses (just one is depicted in Fig. 2) around the parental midpoint. In the case considered here, i.e., up to  $n$  variances, but no covariances, the axes of the hyperellipses are congruent with the coordinate axes.

Two modifications of this scheme have to be mentioned: a simplified version uses just one step-size parameter for all of the object variables. In this case the hyperellipses are reduced to hyperspheres, as depicted in the left part of Fig. 2. A more elaborate *correlated mutation* scheme allows for the rotation of hyperellipses, as shown in the right part of Fig. 2. This mechanism aims at a better adaptation to the topology of the objective function (for details, see [79]).

The settings for the *learning rates*  $\tau$  and  $\tau'$  are recommended as upper bounds for the choice of these parameters (see [126, pp. 167–168]), but one should have in mind that, depending on the particular topological characteristics of the objective function, the optimal setting of these parameters might differ from the values proposed. For the case of one self-adaptable step size, however, Beyer has recently theoretically shown that, for the sphere model (a quadratic bowl), the setting  $\tau_0 \propto 1/\sqrt{n}$  is the optimal choice, maximizing the convergence velocity [127].

The amount of information included into the individuals by means of the self-adaptation principle increases from the simple case of one standard deviation up to the order of  $n^2$  additional parameters, which reflects an enormous degree of freedom for the *internal models* of the individuals. This growing degree of freedom often enhances the global search capabilities of the algorithm at the cost of the expense in computation time, and it also reflects a shift from the precise *adaptation* of a few strategy parameters (as in case of one step size) to the exploitation of a large *diversity* of strategy parameters. In case of correlated mutations, Rudolph [128] has shown that an approximation of the Hessian could be computed with an upper bound of  $\mu + \lambda = (n^2 + 3n + 4)/2$  on the population size, but the typical population sizes  $\mu = 15$  and  $\lambda = 100$ , independently of  $n$ , are certainly not sufficient to achieve this.

The choice of a logarithmic normal distribution for the modification of the standard deviations  $\sigma_i$  is presently also acknowledged in evolutionary programming literature

[129]–[131]. Extensive empirical investigations indicate some advantage of this scheme over the original additive self-adaptation mechanism introduced independently (but about 20 years later than in evolution strategies) in evolutionary programming [132] where

$$\sigma_i^t = \sigma_i \cdot [1 + \alpha \cdot N(0, 1)] \quad (9)$$

(with a setting of  $\alpha \approx 0.2$  [131]). Recent preliminary investigations indicate, however, that this becomes reversed when noisy objective functions are considered, where the additive mechanism seems to outperform multiplicative modifications [133].

A study by Gehlhaar and Fogel [134] also indicates that the order of the modifications of  $x_i$  and  $\sigma_i$  has a strong impact on the effectiveness of self-adaptation: It appears important to mutate the standard deviations first and to use the mutated standard deviations for the modification of object variables. As the authors point out in that study, the reversed mechanism might suffer from generating offspring that have useful object variable vectors but poor strategy parameter vectors because these have not been used to determine the position of the offspring itself.

More work needs to be performed, however, to achieve any clear understanding of the general advantages or disadvantages of one self-adaptation scheme compared to the other mechanisms. A recent theoretical study by Beyer presents a first step toward this goal [127]. In this work, the author shows that the self-adaptation principle works for a variety of different probability density functions for the modification of the step size, i.e., it is an extremely robust mechanism. Moreover, [127] clarifies that (9) is obtained from the corresponding equation for evolution strategies with one self-adaptable step size by Taylor expansion breaking off after the linear term, such that both methods behave equivalently for small settings of the learning rates  $\tau$  and  $\alpha$ , when  $\tau = \alpha$ . This prediction was confirmed perfectly by an experiment reported in [135].

Apart from the early work by Schaffer and Morishima [37], self-adaptation has only recently been introduced in genetic algorithms as a mechanism for evolving the parameters of variation operators. In [37], *punctuated crossover* was offered as a method for adapting both the number and position of crossover points for a multipoint crossover operator in canonical genetic algorithms. Although this approach seemed promising, the operator has not been used widely. A simpler approach toward self-adapting the crossover operator was presented by Spears [136], who allowed individuals to choose between two-point crossover and uniform crossover by means of a self-adaptable operator choice bit attached to the representation of individuals. The results indicated that, in case of crossover operators, rather than adapting to the single best operator for a given problem, the mechanism seems to benefit from the existing diversity of operators available for crossover.

Concerning the mutation operator in genetic algorithms, some effort to facilitate self-adaptation of the mutation rate has been presented by Smith and Fogarty [123], based on earlier work by Bäck [137]. These approaches incorporate the mutation rate  $p_m \in [0, 1]$  into the representation of individuals and allow for mutation and recombination of the mutation rate

in the same way as the vector of binary variables is evolved. The results reported in [123] demonstrate that the mechanism yields a significant improvement in performance of a canonical genetic algorithm on the test functions used.

#### D. Recombination

The variation operators of canonical genetic algorithms, mutation, and recombination are typically applied with a strong emphasis on recombination. The standard algorithm performs a so-called one-point crossover, where two individuals are chosen randomly from the population, a position in the bitstrings is randomly determined as the crossover point, and an offspring is generated by concatenating the left substring of one parent and the right substring of the other parent. Numerous extensions of this operator, such as increasing the number of crossover points [138], uniform crossover (each bit is chosen randomly from the corresponding parental bits) [139], and others, have been proposed, but similar to evolution strategies no generally useful recipe for the choice of a recombination operator can be given. The theoretical analysis of recombination is still to a large extent an open problem. Recent work on *multi-parent recombination*, where more than two individuals participate in generating a single offspring individual, clarifies that this generalization of recombination might yield a performance improvement in many application examples [140]–[142]. Unlike evolution strategies, where it is either utilized for the creation of all members of the intermediate population (the default case) or not at all, the recombination operator in genetic algorithms is typically applied with a certain probability  $p_c$ , and commonly proposed settings of the crossover probability are  $p_c = 0.6$  [13] and  $p_c \in [0.75, 0.95]$  [118].

In evolution strategies recombination is incorporated into the main loop of the algorithm as the first operator (see Algorithm 1) and generates a new intermediate population of  $\lambda$  individuals by  $\lambda$ -fold application to the parent population, creating one individual per application from  $\varrho$  ( $1 \leq \varrho \leq \mu$ ) individuals. Normally,  $\varrho = 2$  or  $\varrho = \mu$  (so-called global recombination) are chosen. The recombination types for object variables and strategy parameters in evolution strategies often differ from each other, and typical examples are *discrete recombination* (random choices of single variables from parents, comparable to uniform crossover in genetic algorithms) and *intermediary recombination* (often arithmetic averaging, but other variants such as geometrical crossover [143] are also possible). For further details on these operators, see [79].

The advantages or disadvantages of recombination for a particular objective function can hardly be assessed in advance, and certainly no generally useful setting of recombination operators (such as the discrete recombination of object variables and global intermediary of strategy parameters as we have claimed in [79, pp. 82–83]) exists. Recently, Kursawe has impressively demonstrated that, using an inappropriate setting of the recombination operator, the (15 100)-evolution strategy with  $n$  self-adaptable variances might even diverge on a sphere model for  $n = 100$  [144]. Kursawe shows that the appropriate choice of the recombination operator not only depends on the objective function topology, but also on the dimension of

the objective function and the number of strategy parameters incorporated into the individuals. Only recently, Rechenberg [46] and Beyer [142] presented first results concerning the convergence velocity analysis of global recombination in case of the sphere model. These results clarify that, for using one (rather than  $n$  as in Kursawe's experiment) optimally chosen standard deviation  $\sigma$ , a  $\mu$ -fold speedup is achieved by both recombination variants. Beyer's interpretation of the results, however, is somewhat surprising because it does not put down the success of this operator on the existence of building blocks which are usefully rearranged in an offspring individual, but rather explains it as a *genetic repair* of the harmful parts of mutation.

Concerning evolutionary programming, a rash statement based on the common understanding of the contending structures as individuals would be to claim that evolutionary programming simply does not use recombination. Rather than focusing on the mechanism of sexual recombination, however, Fogel [145] argues that one may examine and simulate its functional effect and correspondingly interpret a string of symbols as a reproducing population or species, thus making recombination a nonissue (refer to [145] for philosophical reasons underlining this choice).

### E. Selection

Unlike the variation operators which work on the genetic representation, the selection operator is based solely on the fitness values of the individuals.

In genetic algorithms, selection is typically implemented as a probabilistic operator, using the relative fitness  $p(\vec{a}_i) = f(\vec{a}_i) / \sum_{j=1}^{\mu} f(\vec{a}_j)$  to determine the selection probability of an individual  $\vec{a}_i$  (*proportional selection*). This method requires positive fitness values and a maximization task, so that *scaling functions* are often utilized to transform the fitness values accordingly (see, e.g., [18, p. 124]). Rather than using absolute fitness values, *rank-based selection* methods utilize the indexes of individuals when ordered according to fitness values to calculate the corresponding selection probabilities. Linear [146] as well as nonlinear [82, p. 60] mappings have been proposed for this type of selection operator. *Tournament selection* [147] works by taking a random uniform sample of a certain size  $q > 1$  from the population, selecting the best of these  $q$  individuals to survive for the next generation, and repeating the process until the new population is filled. This method gains increasing popularity because it is easy to implement, computationally efficient, and allows for fine-tuning the selective pressure by increasing or decreasing the tournament size  $q$ . For an overview of selection methods and a characterization of their selective pressure in terms of numerical measures, the reader should consult [148] and [149]. While most of these selection operators have been introduced in the framework of a generational genetic algorithm, they can also be used in combination with the steady-state and generation gap methods outlined in Section III.

The  $(\mu, \lambda)$ -evolution strategy uses a deterministic selection scheme. The notation  $(\mu, \lambda)$  indicates that  $\mu$  parents create  $\lambda > \mu$  offspring by means of recombination and mutation, and the best  $\mu$  offspring individuals are deterministically

selected to replace the parents (in this case,  $Q = \emptyset$  in Algorithm 1). Notice that this mechanism allows that the best member of the population at generation  $t + 1$  might perform *worse* than the best individual at generation  $t$ , i.e., the method is not *elitist*, thus allowing the strategy to accept temporary deteriorations that might help to leave the region of attraction of a local optimum and reach a better optimum. In contrast, the  $(\mu + \lambda)$  strategy selects the  $\mu$  survivors from the union of parents and offspring, such that a monotonic course of evolution is guaranteed [ $Q = P(t)$  in Algorithm 1]. Due to recommendations by Schwefel, however, the  $(\mu, \lambda)$  strategy is preferred over the  $(\mu + \lambda)$  strategy, although recent experimental findings seem to indicate that the latter performs as well as or better than the  $(\mu, \lambda)$  strategy in many practical cases [134]. It should also be noted that both schemes can be interpreted as instances of the general  $(\mu, \kappa, \lambda)$  strategy, where  $1 \leq \kappa \leq \infty$  denotes the maximum life span (in generations) of an individual. For  $\kappa = 1$ , the selection method yields the  $(\mu, \lambda)$  strategy, while it turns into the  $(\mu + \lambda)$  strategy for  $\kappa = \infty$  [54].

A minor difference between evolutionary programming and evolution strategies consists in the choice of a probabilistic variant of  $(\mu + \lambda)$  selection in evolutionary programming, where each solution out of offspring and parent individuals is evaluated against  $q > 1$  (typically,  $q \leq 10$ ) other randomly chosen solutions from the union of parent and offspring individuals [ $Q = P(t)$  in Algorithm 1]. For each comparison, a "win" is assigned if an individual's score is better or equal to that of its opponent, and the  $\mu$  individuals with the greatest number of wins are retained to be parents of the next generation. As shown in [79, pp. 96–99], this selection method is a probabilistic version of  $(\mu + \lambda)$  selection which becomes more and more deterministic as the number  $q$  of competitors is increased. Whether or not a probabilistic selection scheme should be preferable over a deterministic scheme remains an open question.

Evolutionary algorithms can easily be ported to parallel computer architectures [150], [151]. Since the individuals can be modified and, most importantly, evaluated independently of each other, we should expect a speed-up scaling linear with the number of processing units  $p$  as long as  $p$  does not exceed the population size  $\mu$ . But selection operates on the whole population so this operator eventually slows down the overall performance, especially for massively parallel architectures where  $p \gg \mu$ . This observation motivated the development of parallel algorithms using local selection within subpopulations like in *migration models* [53], [152] or within small neighborhoods of spatially arranged individuals like in *diffusion models* [153]–[156] (also called *cellular evolutionary algorithms* [157]–[159]). It can be observed that local selection techniques not only yield a considerable speed-up on parallel architectures, but also improve the robustness of the algorithms [46], [116], [160].

### F. Other Evolutionary Algorithm Variants

Although it is impossible to present a thorough overview of all variants of evolutionary computation here, it seems

appropriate to explicitly mention *order-based genetic algorithms* [18], [82], *classifier systems* [161], [162], and *genetic programming* [31], [70], [81], [163] as branches of genetic algorithms that have developed into their own directions of research and application. The following overview is restricted to a brief statement of their domain of application and some literature references:

- *Order-based genetic algorithms* were proposed for searching the space of *permutations*  $\pi: \{1, \dots, n\} \rightarrow \{1, \dots, n\}$  directly rather than using complex decoding functions for mapping binary strings to permutations and preserving feasible permutations under mutation and crossover (as proposed in [164]). They apply specialized recombination (such as *order crossover* or *partially matched crossover*) and mutation operators (such as random exchanges of two elements of the permutation) which preserve permutations (see [82, ch. 10] for an overview).
- *Classifier systems* use an evolutionary algorithm to search the space of *production rules* (often encoded by strings over a ternary alphabet, but also sometimes using symbolic rules [165]) of a learning system capable of induction and generalization [18, ch. 6], [161], [166], [167]. Typically, the *Michigan* approach and the *Pittsburgh* approach are distinguished according to whether an individual corresponds with a single rule of the rule-based system (Michigan) or with a complete rule base (Pittsburgh).
- *Genetic programming* applies evolutionary search to the space of tree structures which may be interpreted as computer programs in a language suitable to modification by mutation and recombination. The dominant approach to genetic programming uses (a subset of) LISP programs (*S* expressions) as genotype space [31], [163], but other programming languages including machine code are also used (see, e.g., [70], [81], and [168]).

Throughout this section we made the attempt to compare the constituents of evolutionary algorithms in terms of their canonical forms. But in practice the borders between these approaches are much more fluid. We can observe a steady evolution in this field by modifying (mutating), (re)combining, and validating (evaluating) the current approaches, permanently improving the population of evolutionary algorithms.

## V. APPLICATIONS

Practical application problems in fields as diverse as engineering, natural sciences, economics, and business (to mention only some of the most prominent representatives) often exhibit a number of characteristics that prevent the straightforward application of standard instances of evolutionary algorithms. Typical problems encountered when developing an evolutionary algorithm for a practical application include the following.

- 1) A suitable representation and corresponding operators need to be developed when the canonical representation is different from binary strings or real-valued vectors.
- 2) Various constraints need to be taken into account by means of a suitable method (ranging from penalty func-

tions to repair algorithms, constraint-preserving operators, and decoders; see [169] for an overview).

- 3) Expert knowledge about the problem needs to be incorporated into the representation and the operators in order to guide the search process and increase its convergence velocity—without running into the trap, however, of being confused and misled by expert beliefs and habits which might not correspond with the best solutions.
- 4) An objective function needs to be developed, often in cooperation with experts from the particular application field.
- 5) The parameters of the evolutionary algorithm need to be set (or tuned) and the feasibility of the approach needs to be assessed by comparing the results to expert solutions (used so far) or, if applicable, solutions obtained by other algorithms.

Most of these topics require experience with evolutionary algorithms as well as cooperation between the application's expert and the evolutionary algorithm expert, and only few general results are available to guide the design of the algorithm (e.g., representation-independent recombination and mutation operators [170], [171], the requirement that small changes by mutation occur more frequently than large ones [48], [172], and a quantification of the selective pressure imposed by the most commonly used selection operators [149]). Nevertheless, evolutionary algorithms often yield excellent results when applied to complex optimization problems where other methods are either not applicable or turn out to be unsatisfactory (a variety of examples can be found in [80]).

Important practical problem classes where evolutionary algorithms yield solutions of high quality include engineering design applications involving continuous parameters (e.g., for the design of aircraft [173], [174] structural mechanics problems based on two-dimensional shape representations [175], electromagnetic systems [176], and mobile manipulators [177], [178]), discrete parameters (e.g., for multiplierless digital filter optimization [179], the design of a linear collider [180], or nuclear reactor fuel arrangement optimization [181]), and mixed-integer representations (e.g., for the design of survivable networks [182] and optical multilayer systems [115]). Combinatorial optimization problems with a straightforward binary representation of solutions have also been treated successfully with canonical genetic algorithms and their derivatives (e.g., set partitioning and its application to airline crew scheduling [183], knapsack problems [184], [185], and others [186]). Relevant applications to combinatorial problems utilizing a permutation representation of solutions are also found in the domains of scheduling (e.g., production scheduling [187] and related problems [188]), routing (e.g., of vehicles [189] or telephone calls [190]), and packing (e.g., of pallets on a truck [191]).

The existing range of successful applications is extremely broad, thus by far preventing an exhaustive overview—the list of fields and example applications should be taken as a hint for further reading rather than a representative overview. Some of the most challenging applications with a large profit potential are found in the field of biochemical drug design, where evolutionary algorithms have gained remarkable interest

and success in the past few years as an optimization procedure to support protein engineering [134], [192]–[194]. Also, finance and business provide a promising field of profitable applications [195], but of course few details are published about this work (see, e.g., [196]). In fact, the relation between evolutionary algorithms and economics has found increasing interest in the past few years and is now widely seen as a promising modeling approach for agents acting in a complex, uncertain situation [197].

In concluding this section, we refer to the research field of *computational intelligence* (see Section VI for details) and the applications of evolutionary computation to the other main fields of computational intelligence, namely fuzzy logic and neural networks. An overview of the utilization of genetic algorithms to train and construct neural networks is given in [198], and of course other variants of evolutionary algorithms can also be used for this task (see e.g., [199] for an evolutionary programming, [200] for an evolution strategy example, and [97] and [201] for genetic algorithm examples). Similarly, both the rule base and membership functions of fuzzy systems can be optimized by evolutionary algorithms, typically yielding improvements of the performance of the fuzzy system (e.g., [202]–[206]). The interaction of computational intelligence techniques and hybridization with other methods such as expert systems and local optimization techniques certainly opens a new direction of research toward hybrid systems that exhibit problem solving capabilities approaching those of naturally intelligent systems in the future. Evolutionary algorithms, seen as a technique to evolve machine intelligence (see [5]), are one of the mandatory prerequisites for achieving this goal by means of algorithmic principles that are already working quite successfully in natural evolution [207].

## VI. SUMMARY AND OUTLOOK

To summarize, the current state of evolutionary computation research can be characterized as in the following.

- The basic concepts have been developed more than 35 years ago, but it took almost two decades for their potential to be recognized by a larger audience.
- Application-oriented research in evolutionary computation is quite successful and almost dominates the field (if we consider the majority of papers). Only few potential application domains could be identified, if any, where evolutionary algorithms have not been tested so far. In many cases they have been used to produce good, if not superior, results.
- In contrast, the theoretical foundations are to some extent still weak. To say it more pithy: “We know that they work, but we do not know why.” As a consequence, inexperienced users fall into the same traps repeatedly, since there are only few rules of thumb for the design and parameterization of evolutionary algorithms.

A constructive approach for the synthesis of evolutionary algorithms, i.e., the choice or design of the representations, variation operators, and selection mechanisms is needed. But first investigations pointing in the direction of design principles for representation-independent operators

are encouraging [171], as well, as is the work on complex nonstandard representations such as in the field of genetic programming.

- Likewise, the field still lacks a sound formal characterization of the application domain and the limits of evolutionary computation. This requires future efforts in the field of complexity theory.

There exists a strong relationship between evolutionary computation and some other techniques, e.g., fuzzy logic and neural networks, usually regarded as elements of artificial intelligence. Following Bezdek [208], their main common characteristic lies in their numerical knowledge representation, which differentiates them from traditional symbolic artificial intelligence. Bezdek suggested the term *computational intelligence* for this special branch of artificial intelligence with the following characteristics<sup>3</sup>:

- 1) numerical knowledge representation;
- 2) adaptability;
- 3) fault tolerance;
- 4) processing speed comparable to human cognition processes;
- 5) error rate optimality (e.g., with respect to a Bayesian estimate of the probability of a certain error on future data).

We regard computational intelligence as one of the most innovative research directions in connection with evolutionary computation, since we may expect that efficient, robust, and easy-to-use solutions to complex real-world problems will be developed on the basis of these complementary techniques. In this field, we expect an impetus from the interdisciplinary cooperation, e.g., techniques for tightly coupling evolutionary and problem domain heuristics, more elaborate techniques for self-adaptation, as well as an important step toward machine intelligence.

Finally, it should be pointed out that we are far from using all potentially helpful features of evolution within evolutionary algorithms. Comparing natural evolution and the algorithms discussed here, we can immediately identify a list of important differences, which all might be exploited to obtain more robust search algorithms *and* a better understanding of natural evolution.

- Natural evolution works under dynamically changing environmental conditions, with nonstationary optima and even changing optimization criteria, and the individuals themselves are also changing the structure of the adaptive landscape during adaptation [210]. In evolutionary algorithms, environmental conditions are often static, but nonelitist variants are able to deal with changing environments. It is certainly worthwhile, however, to consider a more flexible life span concept for individuals in evolutionary algorithms than just the extremes of a maximum life span of one generation [as in a  $(\mu, \lambda)$  strategy] and of an unlimited life span (as in an elitist strategy), by introducing an aging parameter as in the  $(\mu, \kappa, \lambda)$  strategy [54].

<sup>3</sup>The term “computational intelligence” was originally coined by Cercone and McCalla [209].

- The long-term goal of evolution consists of the maintenance of *evolvability* of a population [95], guaranteed by mutation, and a preservation of diversity within the population (the term *meliorization* describes this more appropriately than optimization or adaptation does). In contrast, evolutionary algorithms often aim at finding a precise solution and converging to this solution.
- In natural evolution, many criteria need to be met at the same time, while most evolutionary algorithms are designed for single fitness criteria (see [211] for an overview of the existing attempts to apply evolutionary algorithms to multiobjective optimization). The concepts of *diploidy* or *polyploidy* combined with *dominance* and *recessivity* [50] as well as the idea of introducing two sexes with different selection criteria might be helpful for such problems [212], [213].
- Natural evolution neither assumes global knowledge (about all fitness values of all individuals) nor a generational synchronization, while many evolutionary algorithms still identify an iteration of the algorithm with one complete generation update. Fine-grained asynchronously parallel variants of evolutionary algorithms, introducing local neighborhoods for recombination and selection and a time-space organization like in cellular automata [157]–[159] represent an attempt to overcome these restrictions.
- The *co-evolution* of species such as in predator-prey interactions implies that the adaptive landscape of individuals of one species changes as members of the other species make their adaptive moves [214]. Both the work on competitive fitness evaluation presented in [215] and the co-evolution of separate populations [216], [217] present successful approaches to incorporate the aspect of mutual interaction of different adaptive landscapes into evolutionary algorithms. As clarified by the work of Kauffman [214], however, we are just beginning to explore the dynamics of co-evolving systems and to exploit the principle for practical problem solving and evolutionary simulation.
- The genotype-phenotype mapping in nature, realized by the *genetic code* as well as the *epigenetic apparatus* (i.e., the biochemical processes facilitating the development and differentiation of an individual's cells into organs and systems), has evolved over time, while the mapping is usually fixed in evolutionary algorithms (dynamic parameter encoding as presented in [218] being a notable exception). An evolutionary self-adaptation of the genotype-phenotype mapping might be an interesting way to make the search more flexible, starting with a coarse-grained, volume-oriented search and focusing on promising regions of the search space as the evolution proceeds.
- Other topics, such as multicellularity and *ontogeny* of individuals, up to the development of their own brains (individual learning, such as accounted for by the Baldwin effect in evolution [219]), are usually not modeled in evolutionary algorithms. The self-adaptation of strategy parameters is just a first step into this direction, realizing

the idea that each individual might have its own internal strategy to deal with its environment. This strategy might be more complex than the simple mutation parameters presently taken into account by evolution strategies and evolutionary programming.

With all this in mind, we are convinced that we are just beginning to understand and to exploit the full potential of evolutionary computation. Concerning basic research as well as practical applications to challenging industrial problems, evolutionary algorithms offer a wide range of promising further investigations, and it will be exciting to observe the future development of the field.

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